

AN OPERATOR INEQUALITY IMPLYING CHAOTIC ORDER

M. Ilyas¹, Reyaz Ahmad² & S. Ilyas³

¹*Research Scholar & Head, Department of Mathematics, Gaya College, Gaya, Bihar, India*

²*Research Scholar, American College of Dubai, United Arab Emirates*

³*Research Scholar, Department of Information Technology, Gaya College, Gaya, Bihar, India*

ABSTRACT

This paper proves the assertion that if positive invertible operators A and B satisfy an operator inequality $\left(B^{\frac{t}{2}} A^{\frac{s-t}{2}} B^{s-t} A^{\frac{s-t}{2}} B^{\frac{t}{2}}\right)^{\frac{1}{2s-t}} \geq B$ for $0 < t < \frac{s}{2}$, then by $A \geq B$, if $s < 2 - t$. If $s \geq 2+t$ is additionally assumed then $A \geq B$. A preliminary result Theorem 2 of J.J Fuji, M. Fuji and R. Nakamoto (FFN)[1] is further generalized in Theorem 3.

KEYWORDS: Operator Monotone Function, Operator Inequality, Chaotic Order, Hadamard-Schur Product

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